



**upb.**

ufficio  
parlamentare  
di bilancio

## An integrated approach for the estimation of the Italian output gap

T. Proietti, M. Fioramanti, C. Frale, L. Monteforte

INPS - Palazzo Wedekind, Rome  
12 July 2019

# Roadmap

- Introduction
- The EU framework
- UPB and the OG
- New models for the OG
  - Introduction
  - Selection procedure
  - Models
  - Estimates in real time
  - Results
- Recent OG forecasts
- Conclusion

## Definitions of the potential output

- **Long-term growth:** "The concept of potential output (PO) is generally understood to measure the medium-to-long-term level of sustainable real output in the economy. While measures of potential output growth **abstract from short-term cyclical movements** they can still fluctuate from year to year, reflecting supply conditions" (ECB, MB, Jan 2011).
- **Balanced growth:** "The level of output at which demand and supply in the aggregate economy are balanced so that, all else being equal, **inflation** tends to gravitate to its **long-run** expected value" (Mishkin, speech, 2007).
- **Natural rate:** "Potential output is the rate of output the economy would have if there were **no nominal rigidities** but all other (real) frictions and shocks remained unchanged" (Basu and Fernald, 2009).

# Model uncertainty

Potential output is unobservable, it can only be estimated with **uncertainty**.

- **Modelling**. The potential output may be measured using **statistical** methods (smoothing time series), or by means of **theories** (e.g. the production function) and structural models (cleaning the rigidities); large data-set were also used in the recent literature.
- **Beyond the models**. Large differences arise from the choices of the econometric **specification** and, eventually, also for **a priori and initial conditions**.

# Real time uncertainty

Estimates of potential output are often **revised**, causing sub-optimality of the policies in real-time. The instability is due to various factors:

- **Backward**: data revisions may have an impact on the **whole time series** of potential and output gap.
- **Current**: the end of sample bias of statistical filters affects the real time measures for the **actual values** for potential output.
- **Future**: the end of sample bias may be mitigated considering also **macroeconomic forecasts**, but this comes at the cost of an additional source of uncertainty.

# The EU framework: principles

- 1 It has to be a relatively **simple and fully transparent** methodology, where the key inputs and outputs are clearly delineated.
- 2 **Equal treatment** for all of the EU's Member States needs to be strictly assured.
- 3 Given that the estimates are used for budgetary surveillance purposes, it is important to produce **unbiased estimates** of the past and future evolution of potential growth by seeking to avoid both false optimism or unjustified pessimism.

## The EU framework: the model

- Since 2002 the "official" estimates of the output gap (OG) for the EU countries are produced with a **Commonly Agreed Methodology** (CAM, approved by the ECOFIN); the methodology is continuously revised by the EPC-OGWG.
- The PO is based on the **production function**, where all the main components (except K) are decomposed between the trend and the cycle component.
- Each component (L, K and TFP) is estimated **separately** with different techniques: HP filter, bivariate Kalman filter, Bayesian Kalman filter.
- The model has been criticized because the **potential growth is procyclical**, unstable in real time and strongly affected by **a priori and initial conditions**.

# Why fiscal councils care about PO and OG

- **Long run.** It is important to have a medium-term view of the economic growth, in order to analyse **expenditure plans** and the **debt sustainability**.
- **Medium run.** Output gap is relevant for the most relevant EU's **fiscal rules** (OMT convergence, debt and expenditure rule), other than for inflation projections.
- **Short run.** The output gap is a measure of the **business cycle**, which is relevant for the short term outlook.



## Previous work at UPB: Fioramanti, Padrini and Pollastri (2015)

The research shows that the CAM model has many **drawbacks**, in particular in the NAWRU estimation, related to "minor" details of the model:

- Forecast horizon
- Choice of the software
- Variances' bound of the stochastic processes

They add to the major elements of difference (historical data revision, model choice, differences in forecast) potentially producing huge heterogeneities in potential output and output gap.

For this reason it is key to not only have a point estimate, but an interval/band around a central tendency, possibly obtained with tools taking into account different characteristics of an economy.

## Previous work at UPB: Frale and De Nardis (2018)

- Frale and De Nardis estimate the output gap for Italy, over the period 1985- 2016, based on a **set of models** that uses **UCM**: the signal is extracted from output indicators (GDP, unemployment rate and capacity utilisation) and from a Phillips curve (similar to Jarocinski and Lenza (2016)).
- The selected models differ in their **information sets** and the specification of the **trend**.
- They analyse the **performance** of the different models by comparing them with estimates from international institutions and applying some measures of error.

## Frale and De Nardis (2018): main results

- Alternative forms (trend, information set) of the model produce a **broad range of values for the OG**, confirming the considerable uncertainty characterising this variable.
- The uncertainty surrounding PO and OG is **not eliminated** by adopting a **criterion for assessing the goodness** of the various models: statistical criteria (maximum likelihood or stability of parameters) lead to the selection of different models from those that would be chosen using a more economic criterion, e.g. capacity to forecast inflation.
- **Indeterminacy** depends on the considered period, reflecting particularly the influence exerted by the **recent recession**. Models that appeared optimal prior to the recent economic crisis seem to have lost their explanatory power in recent years.

## New models for the output gap at UPB

- ✓ In a research project led by Tommaso Proietti, we have investigated several methods proposed in the literature: purely statistical, based on the economic theory and hybrid models.
- ✓ However none of them prevails: **each one** has its own **advantages**, in terms of statistical properties, stability of the estimates or economic interpretation.
- ✓ We ended up choosing an **integrated approach** that uses and summarizes all the results coming from **different techniques and econometric specifications**.
- ✓ This allows to construct a **synthetic measure** of PO and OG but also **uncertainty bands** that are particularly useful in the process of fiscal surveillance.

# Selection procedure

We selected the five models accordingly to several criteria:

- **Statistics:** Likelihood, SE, residual diagnostic;
- **Data:** Revisions due to the data;
- **Economics:** Interpretation of the economic relations.

# Selected Models

We selected the five models looking at several properties:

- 1 Bivariate model with **inflation and output**;
- 2 Bivariate model with inflation and output **with shock in the cycle** in 2009;
- 3 Trivariate model with inflation, output and **unemployment**;
- 4 **Multivariate model** in the framework of the production function;
- 5 **Univariate statistical filter calibrated** on the estimates of model 1.

## Other attempts

We have done much more:

- Full replication of **CAM method** and sensitivity analysis to **parameter restrictions** (TFP and NAWRU) ;
- Different variables for **TFP cycle** (e.g. capacity utilization in industry, cig);
- Lower bound for **TFP growth**;
- Time varying parameters of the **Phillips curve**;
- Unemployment net of **demographic trends**;

# Bivariate model with inflation and output

$$y_t = \mu_t + \psi_t, \quad t = 1, \dots, n,$$

$$\begin{aligned} \mu_t &= \mu_{t-1} + \beta_{t-1} + \eta_t, \\ \beta_t &= \beta_{t-1} + \zeta_t, \end{aligned} \quad \text{trend: LLT} \quad \begin{aligned} \eta_t &\sim \text{IIDN}(0, \sigma_\eta^2), \\ \zeta_t &\sim \text{IIDN}(0, \sigma_\zeta^2), \end{aligned}$$

$$\psi_t = \phi_1 \psi_{t-1} + \phi_2 \psi_{t-2} + \kappa_t, \quad \text{cycle: AR(2)} \quad \kappa_t \sim \text{IIDN}(0, \sigma_\kappa^2),$$

$$\begin{aligned} \pi_t &= \gamma_e \pi_t^e + \pi_t^* + \theta_0 \psi_t + \theta_1 \psi_{t-1} + \sum_{k=1}^K \beta_k x_{kt} + \varepsilon_{\pi t}, \\ \pi_t^* &= \pi_{t-1}^* + \eta_{\pi t} \end{aligned} \quad \text{Phillips curve} \quad \begin{aligned} \varepsilon_{\pi t} &\sim \text{IID } N(0, \sigma_{\varepsilon\pi}^2), \\ \eta_{\pi t} &\sim \text{IID } N(0, \sigma_{\eta\pi}^2), \end{aligned}$$

We have investigated different specification for the trend, following Frale and De Nardis (2018).



## Bivariate model with shock in 2009

The residuals of the bivariate model have a clear outlier in 2009, following the burst of the **global financial crisis**. To pick up the special feature of the business cycle in this occasion we allow the bivariate model to include a shock:

- in the level of the trend ( $\mu_t$ )
- in the growth rate of the trend ( $\beta_t$ )
- in the cycle ( $\psi_t$ )

Results in terms of likelihood are very similar, but we recognize a better economic interpretation for the model with the shock in the cycle. Therefore we selected this model, by adding an intervention variable in the specification of the cycle such as:

$$\psi_t = \phi_1 \psi_{t-1} + \phi_2 \psi_{t-2} + \kappa_t + \lambda I(t = \tau), \text{ con } \tau = 2009.$$

# Trivariate model: inflation, output and unemployment

The bivariate model completely neglects the labour market. We thus extend it by adding the Okun(1962) law, that postulates a relation between output gap and unemployment gap. The trivariate model is obtained by adding an equation for Unemployment rate ( $U_t$ ) to the basic structure of the bivariate model. We allow for a more general formulation than the strict proportionality:

$$U_t = \mu_{ut} + \psi_{ut}, \quad t = 1, \dots, n,$$

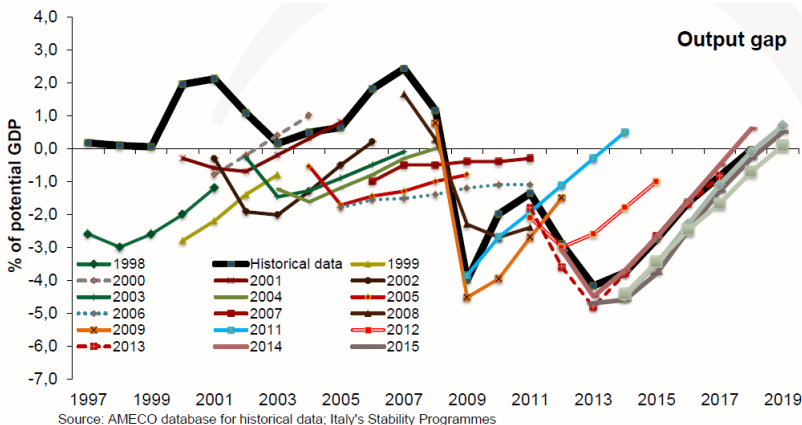
$$\begin{aligned} \mu_{ut} &= \mu_{u,t-1} + \beta_{u,t-1} + \eta_{ut}, & \eta_{ut} &\sim \text{IIDN}(0, \sigma_{\eta_u}^2), \\ \beta_{ut} &= \beta_{u,t-1} + \zeta_{ut}, & \zeta_{ut} &\sim \text{IIDN}(0, \sigma_{\zeta_u}^2), \end{aligned}$$

$$\psi_{ut} = \phi_u \psi_{u,t-1} + \delta_0 \psi_t + \delta_1 \psi_{t-1} + \kappa_{ut}, \quad \kappa_{ut} \sim \text{IIDN}(0, \sigma_{\kappa_u}^2),$$

unemployment gap    output gap

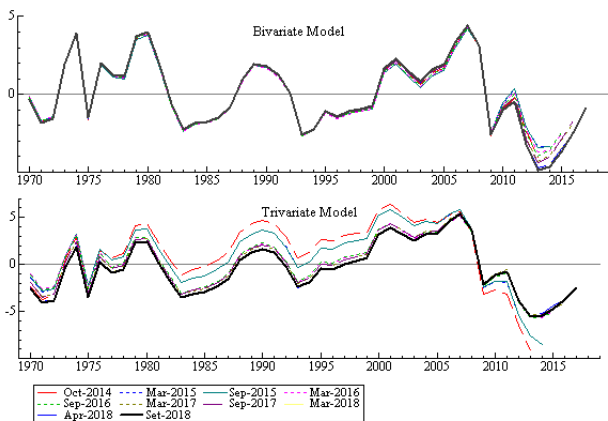
## OG revisions with CAM

Estimates of OG with the EC model are generally revised (sometimes substantially) when new observations are added. This is not desirable in the framework of fiscal surveillance.



## Estimates in real time

We analyse the revisions of our models running a real time experiment.



Results show that the **bivariate** model is **more stable** than the trivariate (adding UR augment the volatility).

# Multivariate integrated model

We propose also a multivariate model in the framework of the production function approach, where all components (labour, capital and TFP) are estimated **simultaneously and efficiently** (exploiting the cross correlation among variables), as proposed by Proietti, Musso and Westerman (2007) and ECB (2018). In this framework the trend and cycle of the output are obtained as combination of the analogues extracted from L, K and TFP:

$$y_t = f_t + \alpha l_t + (1 - \alpha)k_t = \mu_t + \psi_t$$

$$\mu_t = \mu_{ft} + \alpha(\mu_{ht} + \mu_{at} + \mu_{et} + p_t) + (1 - \alpha)k_t \quad \text{trend}$$

$$\psi_t = \psi_{ft} + \alpha(\psi_{ht} + \psi_{at} + \psi_{et}) \quad \text{cycle}$$

Thus the usual state space form is derived.

# Multivariate integrated model

Given  $Y_t = (f_t, a_t, h_t, e_t, c_t)'$ , where  $f_t$  is the Solow residual,  $a_t$  the participation rate,  $h_t$  hours worked per capita,  $e_t$  the employment rate and  $c_t$  is the CUBS, and given  $\mu_t = (\mu_{ft}, \mu_{ht}, \mu_{at}, \mu_{et})'$ ,  $\psi_t = (\psi_{ft}, \psi_{ht}, \psi_{at}, \psi_{et})'$ ,  $\Psi_t = \gamma' \psi_t$ ,  $\gamma = (1, \alpha, \alpha, \alpha)'$  we have:

$$Y_t = \mu_t + \psi_t \quad t = 1, \dots, n,$$

$$\mu_t = \mu_{t-1} + \beta_{t-1}$$

$$\beta_t = \beta_{t-1} + \zeta_t$$

$$\zeta_t \sim \text{IIDN}(0, \Sigma_\zeta)$$

$$\psi_t = \phi_1 \psi_{t-1} + \phi_2 \psi_{t-2} + \kappa_t$$

$$\kappa_t \sim \text{IIDN}(0, \Sigma_\kappa),$$

$$c_t = \theta_c \psi_{ft} + \varepsilon_{ct}$$

TFP cycle: CUBS

$$\varepsilon_{ct} \sim \text{IID } N(0, \sigma_{\varepsilon c}^2),$$

$$\pi_t = \gamma_e \pi_t^e + \pi_t^* + \theta_0 \psi_t + \theta_1 \psi_{t-1} + \sum_{k=1}^K \beta_k x_{kt} + \varepsilon_{\pi t},$$

$$\varepsilon_{\pi t} \sim \text{IID } N(0, \sigma_{\varepsilon \pi}^2),$$

$$\pi_t^* = \pi_{t-1}^* + \eta_{\pi t}$$

$$\eta_{\pi t} \sim \text{IID } N(0, \sigma_{\eta \pi}^2),$$

$\Sigma_\zeta$  is diagonal, whereas  $\Sigma_\kappa$  is full. The multivariate cycle has scalar coefficients that are the same of the OG. The CUBS indicator is a combination of survey data on capacity utilization, and business confidence, as done by EC.

# Statistical filter

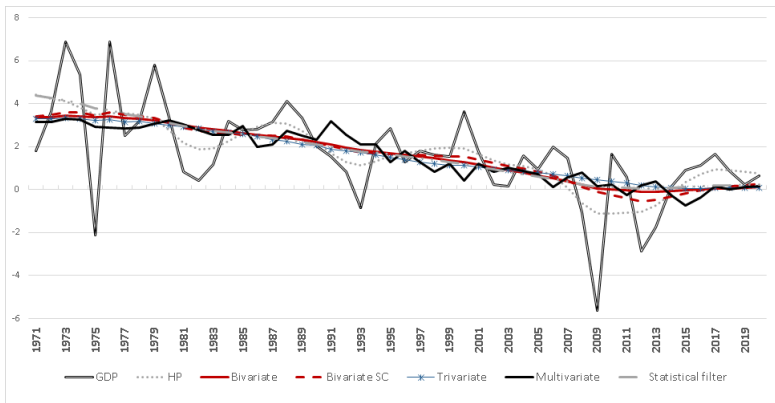
- Starting from the production function  $y_t = f_t + \alpha l_t + (1 - \alpha)k_t$  a simpler way to compute potential output is applying a **univariate statistical filter to each component**.
- The Hodrick and Prescott (1997) filter is the most used in this literature. HP is simple, but completely predefined and affected by the end of point bias.
- We use a **specific filter**, similar to HP, but set in order to mimic the cycle component of GDP, as derived from the bivariate model presented before (which appears to be quite stable in real time).
- This is easily accomplish by using a standard (LLT) model trend+cycle for GDP with the following **restrictions**:

$$\sigma_{\eta}^2 = 0, \sigma_{\zeta}^2 = 0.0168\sigma_K^2, \rho = 0.56, \lambda_c = 0.04,$$

where  $\rho$  is the damping factor and  $\lambda_c$  the cycle frequency (remind:  $\phi_2 = -\rho^2$ ;  $\phi_1 = 2\rho \cos \lambda_c$ ).

# Results: Potential output (1)

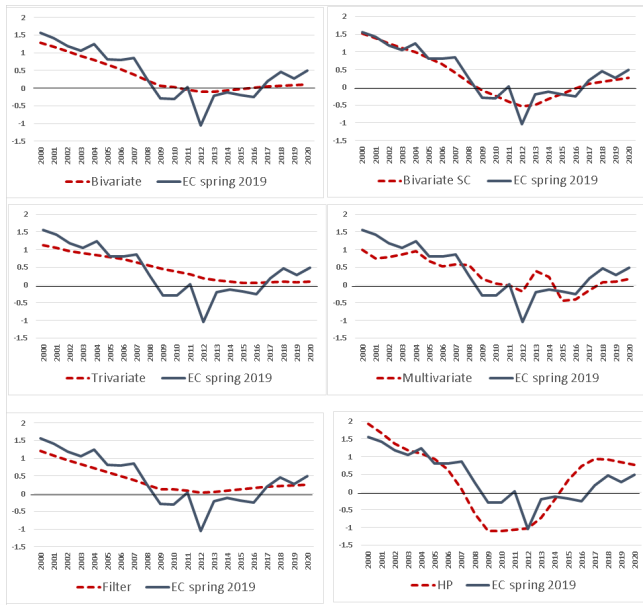
Figure: GDP and potential growth in the different models



There is a clear **downside trend** in potential output in all models, which is coherent with weak GDP growth.



## Potential output (2): UPB models and CAM (2019 estimates)

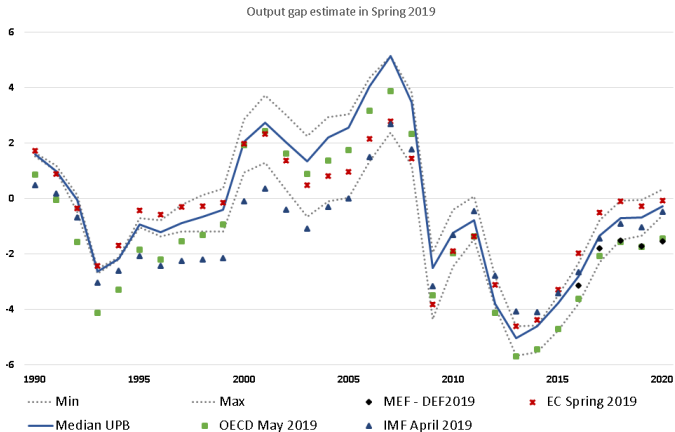


## Results: Potential output (3)

- ✓ The **bivariate** model with the **shock** estimates a stronger reduction in potential output during the last big recession but it appears **more volatile** than the simple bivariate as it provides a stronger rebound in recent years.
- ✓ The **Trivariate** model produces a **smoother potential**: part of the downturn in the recession period is assigned to the unemployment gap. In current years a relevant part of the unemployment is still considered temporary and thus the output gap results smaller than the same computed by the bivariate model.
- ✓ Results from the **multivariate model** are the most volatile; after 2015 the potential growth is limited by the capacity utilization dynamics.
- ✓ The **statistical filter** produces **intermediate results** from the trivariate and bivariate models.
- ✓ PO of UPB models are **less volatile** than those of **HP** and **CAM**.

# Results: OG forecasts (1)

- UPB uses the 5 models (along with CAM and HP) in order to evaluate the Government projections; the models are combined in order to derive a **synthetic measure** but also a **plausibility band**.
- The 5 models are **integrated** with the other tools used at UPB for the validation.



## Results: OG forecasts (2)

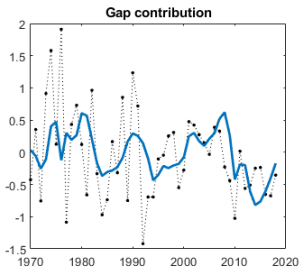
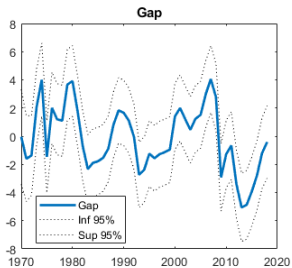
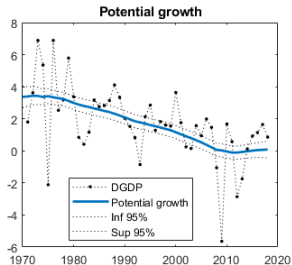
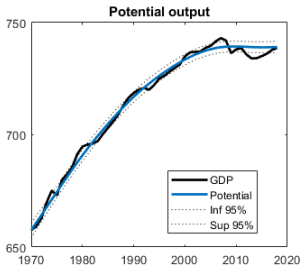
- ✓ We compare our OG estimates computed in **Spring 2019** with those produced by the Government and EC. The macroeconomic framework is quite similar: GDP is foreseen to increase very modestly by all institutions, especially in 2019 (around 0,1 per cent).
- ✓ The median OG by UPB models is quite close to the measure provided by **EC: turning points are almost coincident**. Tough potential output estimated by UPB is less procyclical and the resulting OG more volatile.
- ✓ **EC** estimates lie **almost always in the range** between maximum and minimum of UPB models.
- ✓ Also **Government** estimates are **inside** the plausibility band, but **only up to 2019**, while afterwards they appear to be smaller (wider negative OG) than those produced by UPB.

## Summary and conclusion

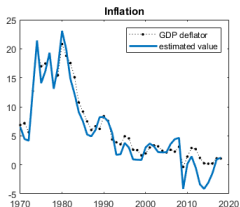
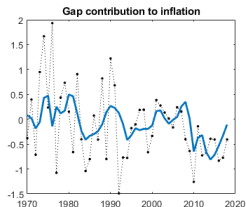
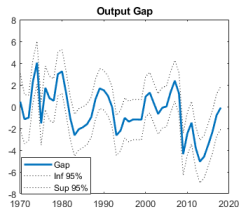
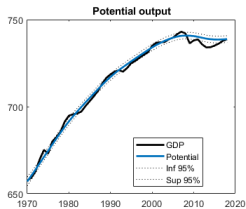
- ✓ We develop **new models** for the potential output and the output gap of the Italian economy, that encompass different economic and statistical approaches.
- ✓ The models are relatively **robust to data revision** in real time.
- ✓ We construct **uncertainty measures** based on the heterogeneity of the estimates across models.
- ✓ The median output gap of the new models is **between the estimates of the EC and the MEF** up to this year; more oriented toward the EC values in 2020.

Thank you for attention!

# Bivariate Model

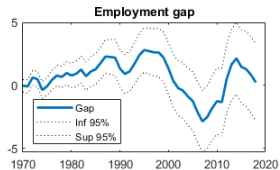
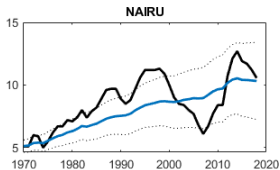
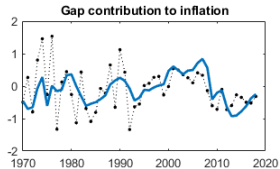
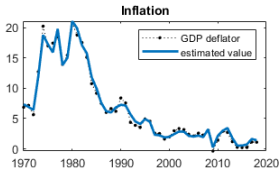
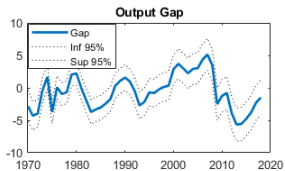
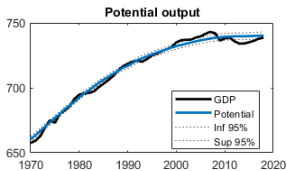


# Bivariate Model with shock

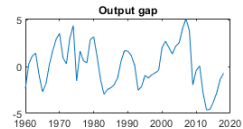
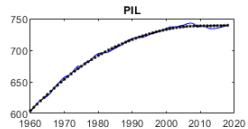
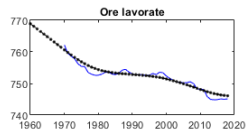
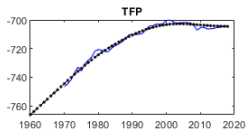




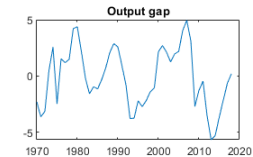
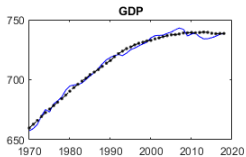
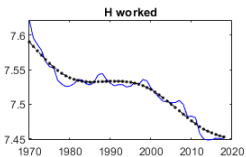
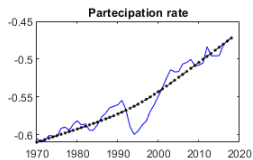
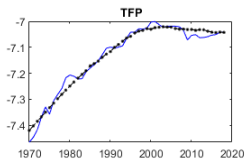
# Trivariate Model



# Filter



# Multivariate Model



# Multivariate Model Gaps

